

# 11-th Balkan Mathematical Olympiad

Novi Sad, Yugoslavia – May 10, 1994

1. An acute angle  $XAY$  and a point  $P$  inside it are given. Construct (by a ruler and a compass) a line that passes through  $P$  and intersects the rays  $AX$  and  $AY$  at  $B$  and  $C$  such that the area of the triangle  $ABC$  equals  $AP^2$ . *(Cyprus)*

2. Let  $m$  be an integer. Prove that the polynomial

$$x^4 - 1994x^3 + (1993 + m)x^2 - 11x + m$$

has at most one integer zero. *(Greece)*

3. Let  $(a_1, a_2, \dots, a_n)$  be a permutation of the numbers  $1, 2, \dots, n$ , where  $n \geq 2$ . Determine the largest possible value of

$$\sum_{k=1}^{n-1} |a_{k+1} - a_k|. \quad \text{span style="float: right;">*(Romania)*$$

4. Find the smallest number  $n > 4$  for which there can exist a set of  $n$  people, such that any two people who are acquainted have no common acquaintances, and any two people who are not acquainted have exactly two common acquaintances. (Acquaintance is a symmetric relation.)

*(Bulgaria)*